

2018–19 Autumn

MATH115 Basic Mathematics - Homework 3

N. Course

DEADLINE: Tuesday 23 October 2018, 3pm

Exercise 11 (Differentiation Rules).

(a) Find
$$y''$$
 if $y = 3x^7 - 7x^3 + 21x^2$.

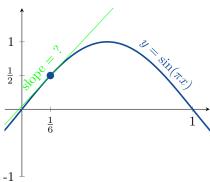
(b) Find
$$\frac{db}{dz}$$
 if $b = -2z^{-1} + \frac{4}{z^2}$.

Exercise 12 (Derivatives of Trigonometric Functions). Calculate the following derivatives. Simplify your answers.

(a) Find
$$\frac{dr}{d\theta}$$
 if $r = (1 + \sec \theta) \sin \theta$.

(b) Find
$$\frac{d^3}{dx^3} \left(-2\sin x \right) \bigg|_{x=\pi}$$
.

Exercise 13 (Slope of a Function). Find the slope of the graph $y = \sin(\pi x)$ at the point $(\frac{1}{6}, \frac{1}{2})$.



Exercise 14 (Differentiation Rules). Find $\frac{dy}{dx}$ if $y = \frac{x^2 + 3}{(x-1)^3 + (x+1)^3}$. (Please simplify your answer.)

Exercise 15 (The Chain Rule).

(a) Differentiate $y = (5 - 2x)^{-3} + \frac{1}{8} \left(\frac{2}{x} + 1\right)^4$.

(b) Differentiate $p = \sqrt{3t + t \sin 3t}$.