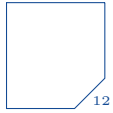
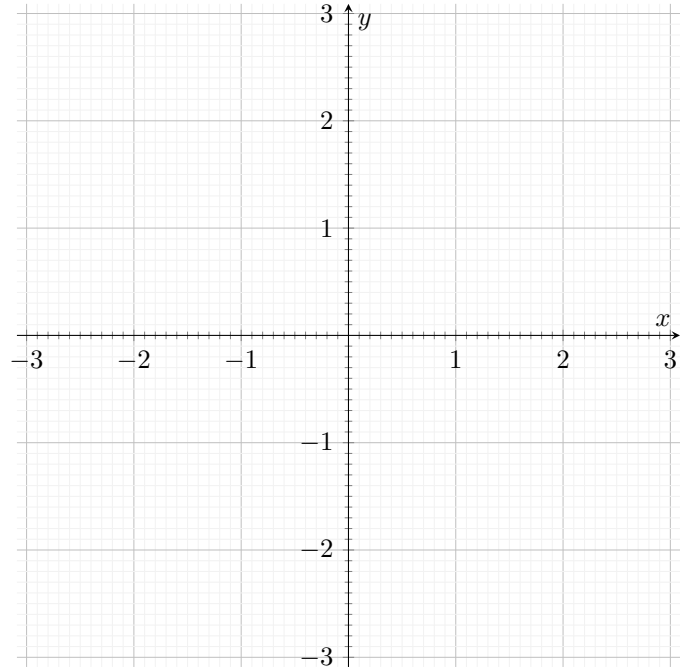
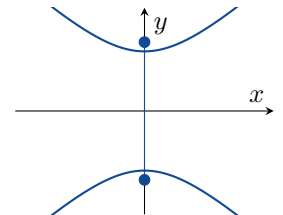
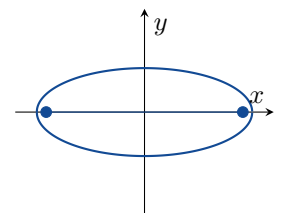


FORENAME: SURNAME: STUDENT NO: 

2018–19 Autumn

MATH115 Basic Mathematics – Homework 6

N. Course

**DEADLINE: Tuesday 4 December 2018, 3pm****Exercise 26 (Polar Coordinates).**(a) Find Cartesian coordinates  $(x, y)$  for the polar coordinates  $(r, \theta) = (\sqrt{8}, 315^\circ)$ .(c) Draw the set of points whose polar coordinates satisfy  $1 \leq r \leq 3$  and  $45^\circ \leq \theta \leq 180^\circ$ .(b) Find polar coordinates  $(r, \theta)$  for the Cartesian coordinates  $(x, y) = (-\frac{\sqrt{27}}{2}, \frac{3}{2})$ .**Exercise 27 (Conic Sections).**(a) Find the focus of the hyperbola  $\frac{y^2}{48} - x^2 = 1$ .(b) Find the foci of the ellipse  $5x^2 + 30y^2 = 150$ .

**Exercise 28 (Three Dimensional Coordinate Systems).** Find the centre and the radius of the sphere

$$8z + 2x^2 + 88 + 2y^2 + 2z^2 = 28y.$$

**Exercise 29 (Vectors).** Let  $\mathbf{a} = 2\mathbf{i} + \mathbf{j}$ ,  $\mathbf{b} = -2\mathbf{i} + 3\mathbf{j}$  and  $\mathbf{c} = 2\mathbf{i} - 11\mathbf{j}$ .

(a) Find  $(5\mathbf{a} - 3\mathbf{b})$ .

(b) Find  $(2\mathbf{a} + 3\mathbf{b} + \mathbf{c})$  and  $\|2\mathbf{a} + 3\mathbf{b} + \mathbf{c}\|$ .

**Exercise 30 (Vectors).** Find a unit vector which points in the same direction as  $\mathbf{v} = 32\mathbf{i} + 30\mathbf{j} - 24\mathbf{k}$ .